

Flow Transport Phenomena of a Hybrid Nanofluid Suspended by Magnetic Iron Oxide and Molybdenum Disulfide Nanoparticles in Blood Plasma

Gopi Vinayagam ¹ , Vijaya Kumar Avula Golla ^{1,*} 

¹ Department of Mathematics, SAS, Vellore Institute of Technology, Vellore-632014, India; gopi.v2018@vitstudent.ac.in (G.V); vijayakumarag@vit.ac.in (V.K.A.G);

* Correspondence: vijayakumarag@vit.ac.in (V.K.A.G.);

Scopus Author ID8227441000

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Abstract: This present work reveals the numerical solution of two-dimensional MoS₂-Fe₃O₄/blood-based hybrid nanofluid flow over a stretching surface with affecting thermal radiation. Iron oxide (Fe₃O₄) and Molybdenum Disulfide (MoS₂) are hybrid nanoparticles that are suspended in blood plasma. This investigation provides information on the effectiveness of distinct physical quantities such as thermal radiation, dissipative viscosity, heat absorption, and convective heat transfer. Various parameters and their effects on temperature and velocity are examined in this explanatory paper. The explanations using graphs and numerical tables aid in understanding and strengthen interpretations of the study's findings. A flow transport model constructs coupled partial differential equations, which may be transformed into ordinary differential equations by appropriate similarity transformations. The R-K-Felberg-integration through shooting technique is then used to elucidate the resulting equations numerically. Based on these findings, the heat transmission rate of MoS₂-Fe₃O₄/Blood is superior to that of Fe₃O₄/blood subject to thermal radiation.

Keywords: MoS₂ -Fe₃O₄/blood; magnetic field; hybrid nanofluid; heat source absorption; thermal radiation; porous medium.

Nomenclature:

B_i	Biot Number	R	Radiation Parameter
B_0	Strength of magnetic field (T)	T	Temperature of the fluid
C_{f_x}	Skin friction coefficient	T_w	Temperature of the surface (K)
C_p	Specific heat ($Jkg^{-1}K^{-1}$)	T_∞	Ambient temperature (K)
ρC_p	Heat capacity	u_w	Stretching surface velocity (ms^{-1})
E_c	Eckert Number	u_∞	Mainstream velocity
$f(\eta)$	Dimensionless velocity function	α	Thermal diffusivity
k	Thermal conductivity ($Wm^{-1}K^{-1}$)	ϕ	Volume fraction
k^*	Rosseland mean absorption coefficient (m^{-1})	μ	Dynamic viscosity ($kgm^{-1}s^{-1}$)
M	Magnetic field	f	Base fluid
P_r	Prandtl number	ρ	Density
Q_0	Heat source/Sink coefficient	hnf	Hybrid Nanofluid

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1. Introduction

Blood is the fluid that transports oxygen, nutrients, and other metabolic wastes throughout the body to preserve cell-level metabolism, regulate the human body's pH, osmotic pressure, and temperature, and protect it from microbial and mechanical harm. Human blood, which comprises erythrocytes, leukocytes, and platelets suspended in plasma, is a Newtonian fluid that is heterogeneous and polyphasic. However, due to the suspension, the entire blood has non-Newtonian fluid characteristics, which substantially alters natural philosophy aspects. The flow of the blood traveling through massive blood vessels Newtonian behavior may be presumed. On the other hand, blood has a non-Newtonian nature in narrow arteries or capillaries. Blood is employed as a testing medium since the medications are made in the form of a hybrid nanofluid. In addition, hybrid nanofluid is improving the thermal efficiency of the base fluid. Normal viscosity and temperature are required for superior blood circulation to promote consistency in blood transmission. The nanoparticles are widely employed in food products, medical science, nuclear furnace, farming, and other fields. The primary convective fluids, like air, oils, H₂O, C₂H₆O₂, etc., have the lowest thermal conductivity. Therefore nanofluids are discovered for better thermal conductivity.

The name nanofluid was early proposed by Choi [1, 2] and is explained as the fluids between 1-100 nm in size disseminated in the base fluid. From the early 1990s onwards, numerous nanofluid research papers have been published. Eshetu Heile *et al.* [3] studied two types of nanofluids Cu/water and Al₂O₃/water by means of portable permeable surface and described Blasius and Sakiadis velocity profiles for both Cu and Al₂O₃. The influence of radiation on Copper (Cu)-water and Silver (Ag)-water nanofluids on a stretching surface a constant for stable magnetohydrodynamics investigation was conducted numerically by Elazem *et al.* [4] and discovered that Silver (Ag)-water nano liquid has greater thermal conductivity and temperature than Copper (Cu)-water nano liquid. Gaikwad *et al.* [5] investigated two different types of nano liquids, Cu-water and CuO-water, over the vertical permeable stretched flat plate with a heat source and noticed that the Copper-water nanofluid is effectively embellishing heat transfer with Copper oxide-water nanofluid. The numerical investigation of three different nanofluids, Aluminium oxide/water, Copper oxide/water, and Copper/water flow through a square cross-cut pipe, was deliberated by Heris *et al.* [6] and observed that Copper-water has higher energy transfer characteristics. In contrast, Copper Oxide-water has a moderate energy transfer rate, and Aluminium Oxide-water has the lowest energy transfer rate. Further, numerical analysis of the free convective transmission of heat characteristics of Ag-water nano liquid in a cage with the center heater at both horizontal and vertical positions has been explored by Nithyadevi *et al.* [7].

However, the researcher is searching for an advanced type of nanofluid, such as a hybrid nanofluid. A Hybrid nanofluid is a mixture of two or more different particles of nanometre size with base fluids and has better thermal conductivity enhanced heat transfer than nanofluids. Recently Indumathi *et al.* [8] investigated three different types of hybrid nanofluids, Al₂O₃-TiO₂/H₂O, Al₂O₃-SiO₂/H₂O, and TiO₂-SiO₂/H₂O with Marangoni boundary constraints and observed that Al₂O₃-TiO₂/H₂O has higher temperature rate than Al₂O₃-SiO₂/H₂O and TiO₂-SiO₂/H₂O. Anjali Devi *et al.* [9] investigated hydromagnetic hybrid nano liquid Cu-Al₂O₃/water through an absorbing stretching surface under the nose of a magnetic field numerically and discovered that the thermal energy rate of Copper-Aluminium Oxide /water is greater than that of Copper/water in magnetic flux. Rajesh *et al.* [10] deliberated the unstable

free convection boundary layer stream of Copper-Aluminium Oxide/water caused due to stretching surface under the influence of magnetohydrodynamic effects. Rusya Iryanti Yahaya *et al.* [11] investigated the stream and energy dissipation of a hybrid nanofluid Copper-Aluminium Oxide/water through an absorbing stretching or shrinking surface. W. Alghamdi *et al.* [12] investigated the flow of Copper-Copper Oxide/Blood hybrid nano liquid with coupling stress over a permeable path through a rectangular field and discovered the pressure dispersion while the drug consignment maintained the vessel's blood flow stability. The stability and numerical solutions of 3D rotating hybrid nanofluid (Cu-Al₂O₃/Water) flow have been studied by Nursya Zana Anuar *et al.* [13]. And produced a non-unique solution when $\lambda \leq -1$, the distinct solution has been observed when $\lambda > -1$ and no solutions exist otherwise. Iskandar Waini *et al.* [14] looked into a hybrid nanofluid (Cu-Al₂O₃/H₂O) over a permeable, non-uniformly stretching and shrinking surface with consequences of thermal radiation. Nursyahirah Wahid *et al.* [15] have recently scrutinized a hybrid nanofluid (Alumina-copper/water) slipstream caused by a stretching and shrinking surface that can generate heat exponentially. Afterward, Muhammad Ijaz Khan *et al.* [16] examined entropy optimization in magnetohydrodynamic hybrid nanofluid (SiO₂-MoS₂/C₃H₈O₂) flow towards a stretchable surface. Investigation of Marangoni hybrid nanofluid (Cu-Al₂O₃/Water) protective layer flow over a bibulous infinite disc plunged in a porous medium was studied by Nursyahirah Wahid *et al.* [17]. Nurul Amira Zainal *et al.* [18] have recently studied an unsteady hybrid nano liquid (Alumina-copper/water) at the point of stagnation with the inclusion of electro magneto hydrodynamic over a stretching/shrinking sheet. The consequential effects of absorption and magnetic field through a moving plate of a hybrid nano liquid Cu-Al₂O₃/water were examined numerically by NuradilahLiyana Aladdin *et al.* [19]. Aly and Pop [20] investigated magnetohydrodynamics, thermal radiation, and mixed convection of the wall jet flow for a hybrid nanofluid Cu-Al₂O₃/water over a vertical plate. The heat transfer and rheological properties of (Ag-CuO/water) through a moving oscillating cylinder were explored numerically by Rajesh *et al.* [21], who noticed that Ag-CuO/water achieves superior temperatures but lower velocities than CuO/water.

Hamza Babar *et al.* [22] discussed the Preparation, Thermophysical properties, diligence, and contradictions of hybrid nanofluid. Suresh *et al.* [23, 24] empirically scrutinized the Al₂O₃-Cu nanocomposite powder developed by thermochemical process and Al₂O₃-Cu/water proposed by scattering the enzymatic nanocomposite powder in purified H₂O. Theoretical and software development results in a problem-solving environment that allow them to solve boundary value problems faster has been explained by Jacek and Shampine [25]. Hayat *et al.* [26] explored 3-D the magnetohydrodynamic flow of circulatory hybrid nanofluid Ag-CuO/water over a stretching field with heat propagation or suction effects. Afterward, Nadeem *et al.* [27] studied the heat transmission of a hybrid nanofluid within the sight of nanoparticles of SWCNT-MWCNT over a 3-D convectively heated stretching environment. The MHD flow and heat transmission of hybrid nano liquid Cu-Al₂O₃/water suspended in the micropolar grubby fluid under the nose of shapes nanoparticles analysis has been made by Hosseinzadeh *et al.* [28]. Afridi *et al.* [29] have scrutinized the Blasius (infinite static plate) and Sakiadis (moving flat plate) flows of hybrid nanofluids Cu-Al₂O₃/H₂O and Cu-Al₂O₃/paraffin Oil under the nose of viscous dissipation. Recently Mumtaz Khan *et al.* [30] explored the continuous 3D combined convective mechanism flow past a stretching perpendicular surface of uneven compactness slip effects, plunged in a permeable material congested with hybrid nanofluid (MoS₂-SiO₂/water). Afterward, Mahato *et al.* [31] studied the

effectiveness of magnetic dipole on the MHD flow of an electrically conducting hybrid nanofluid $\text{MoS}_2\text{-SiO}_2/\text{EG}$ among two infinite perpendicular parallel plates under the nose of a rotating frame. Hussain [32] studied explorations of the flow characteristics of an ethylene-glycol-based hybrid nanofluid, including graphene- MoS_2 using numerical and statistical methods. The flows of an electro-hydrodynamic couple stress hybrid nanofluid (SWCNT-MWCNT/blood) through a stretching surface were analyzed by Anwar Saeed *et al.* [33]. In the presence of an external radial magnetic field, J Tripathi *et al.* [34] deliberated theoretical and numerical solutions of the magneto hemodynamics through a diseased artery with (Ag-Au/blood) overlapping stenosis. Hassan Waqas *et al.* [35] scrutinized the radiative flow of hybrid nanofluids containing aluminum alloys AA7072-AA7075 between two continuously rotating surfaces. A substantial influence of magnetic field on the 2D flow of couple stress hybrid nanofluid $\text{TiO}_2\text{-Ag/blood}$ movement of combined convective mechanism across a spinning sphere in the submerging of MHD was explored by Taza Gul *et al.* [36]. H.S. Chahregh *et al.* [37] have investigated the hydrodynamic/thermal interpretation of arterial blood circulation in the appearance of titanium and silver nanoparticles. Some references are included on various topics related to MHD using nanofluid[38-53].

Inspired by the above literature, we explored the Numerical study of hybrid nanofluid ($\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$) flows to accomplish a stretching sheet by means of a porous medium with thermal radiation. By referring to the work of Devi and Devi. [9] a mathematical formulation of the present article flourished. The nonlinear partial differential equations of the governing flow were transformed into nonlinear ordinary differential equations, which can then be, worked out numerically employing the similarity transformation method. This study explores the effects of magnetic parameters, heat generation, radiation parameters, Eckert number, Biot number, and the effects of nanoparticle volume proportion on skin friction and the Nusselt number with temperature and velocity patterns.

2. Mathematical Analysis

Consider a steady two - dimensional flow of $\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$ towards a porous stretching sheet under the nose of thermal radiation and magnetic field, were investigated. The system of rectilinear coordinates and the corporeal representation of the contemporary investigation are illustrated in Figure 1; the horizontal axis represents the orientation of the stretching sheet, while the vertical axis is perpendicular to the stretching sheet.

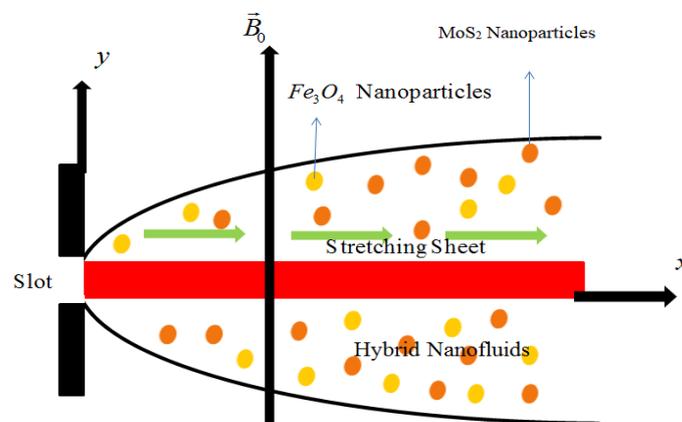


Figure 1. Physical configuration of the problem.

The stretching surface has the velocity $U_w(x) = ax$, where a denotes the constant velocity of the sheet. The wall is permeable with porous. The stretching sheet is subjected to an induced magnetic flux \vec{B}_0 that is orthogonal to the sheet. The sheet surface is kept at a temperature T_w that is higher than the ambient temperature T_∞ .

In steady state, the presidential equations of mass, momentum, and energy, as well as the partial differential equations, can be expressed using the aforesaid considerations as the continuity equation:

$$u_x + v_y = 0 \tag{2.1}$$

$$\rho_{hmf} (uu_x + vv_y) = \mu_{hmf} u_{yy} - \sigma_{hmf} B_0^2 u - \mu_{hmf} \frac{u}{k} \tag{2.2}$$

$$(\rho c_p)_{hmf} (uT_x + vT_y) = k_{hmf} T_{yy} - (q_r)_y + \mu_{hmf} u_y^2 + Q_0(T - T_\infty) \tag{2.3}$$

The boundary conditions for governing equations (2.1), (2.2), and (2.3) is:

$$u(x) = u_w(x) = ax, -k_{hmf} \frac{\partial T}{\partial y} = h_f (T_w - T), v(x) = 0 \text{ When } y(x) = 0 \tag{2.4}$$

$$u(x) \rightarrow 0, T \rightarrow T_\infty \text{ When } y(x) \rightarrow \infty \tag{2.5}$$

where a is a constant, the components of velocity in the x and y directions respectively, are represented by u and v , μ_{hmf} is the effective dynamic viscosity, ρ_{hmf} is the effective density, σ_{hmf} is represented by the electric conductivity, $(c_p)_{hmf}$ is the specific heat and k_{hmf} corresponds to the hybrid nanoliquid's thermal conductivity, T denote the temperature of the fluid, T_w corresponds to the wall's temperature and T_∞ denotes the ambient temperature.

Table 1. Thermo physical traits of MoS₂-Fe₃O₄/blood.

Properties	Nanofluid	Hybrid Nanofluid
Density	$\rho_{nf} = (1-\phi)\rho_f + \phi\rho_{Fe_3O_4}$	$\rho_{hmf} = (1-\phi_2)\{(1-\phi_1)\rho_f + \phi_1\rho_{Fe_3O_4}\} + \phi_2\rho_{MoS_2}$
Viscosity	$\mu_{nf} = \frac{\mu_f}{(1-\phi)^{2.5}}$	$\mu_{hmf} = \frac{\mu_f}{(1-\phi_1)^{2.5}(1-\phi_2)^{2.5}}$
Electric conductivity	$\frac{\sigma_{nf}}{\sigma_f} = \frac{\sigma_{Fe_3O_4} + 2\sigma_f - 2\phi(\sigma_f - \sigma_{Fe_3O_4})}{\sigma_{Fe_3O_4} + 2\sigma_f + \phi(\sigma_f - \sigma_{Fe_3O_4})}$	$\frac{\sigma_{hmf}}{\sigma_{bf}} = \frac{\sigma_{MoS_2} + 2\sigma_{bf} - 2\phi_2(\sigma_{bf} - \sigma_{MoS_2})}{\sigma_{MoS_2} + 2\sigma_{bf} + \phi_2(\sigma_{bf} - \sigma_{MoS_2})}$ $\frac{\sigma_{bf}}{\sigma_f} = \frac{\sigma_{Fe_3O_4} + 2\sigma_f - 2\phi_1(\sigma_f - \sigma_{Fe_3O_4})}{\sigma_{Fe_3O_4} + 2\sigma_f + \phi_1(\sigma_f - \sigma_{Fe_3O_4})}$
Heat Capacity	$(\rho c_p)_{nf} = (1-\phi)(\rho c_p)_f + \phi(\rho c_p)_{Fe_3O_4}$	$(\rho c_p)_{hmf} = (1-\phi_2)[(1-\phi_1)(\rho c_p)_f + \phi_1(\rho c_p)_{Fe_3O_4}] + \phi_2(\rho c_p)_{MoS_2}$

Properties	Nanofluid	Hybrid Nanofluid
Thermal Conductivity	$\frac{k_{nf}}{k_f} = \frac{k_{Fe_3O_4} + 2k_f - 2\phi(k_f - k_{Fe_3O_4})}{k_{Fe_3O_4} + 2k_f + \phi(k_f - k_{Fe_3O_4})}$	$\frac{k_{hnf}}{k_{bf}} = \frac{k_{MoS_2} + 2k_{bf} - 2\phi_2(k_{bf} - k_{MoS_2})}{k_{MoS_2} + 2k_{bf} + \phi_2(k_{bf} - k_{MoS_2})}$ $\frac{k_{bf}}{k_f} = \frac{k_{Fe_3O_4} + 2k_f - 2\phi_1(k_f - k_{Fe_3O_4})}{k_{Fe_3O_4} + 2k_f + \phi_1(k_f - k_{Fe_3O_4})}$

Table 2. Thermophysical characteristics of $MoS_2 - Fe_3O_4$ /blood.

Main Features	$\rho(kg / m^3)$	$c_p (J / kgK)$	$k(W / mk)$	$\sigma(s / m)$
Blood	1060	3770	0.492	4.3×10^{-5}
Molybdenum Disulfide MoS_2	5060	397.21	904.4	2.09×10^{-4}
Ferrosferric oxide Fe_3O_4	5200	670	6	25000

By introducing the following similarity variables:

$$u = axf'(\eta), v = -(av_f)^{\frac{1}{2}} f(\eta), \eta = \left(\frac{a}{v_f}\right)^{\frac{1}{2}} y, T - T_\infty = (T_w - T_\infty)\theta(\eta) \tag{2.6}$$

The emissive heat flux is expressed by means of the Rosseland approximation for radiation as:

$$q_r = -\frac{4\sigma^*}{3k^*} \frac{\partial T^4}{\partial y} \tag{2.7}$$

where the constant for Stephen-Boltzmann and the coefficient of Rosseland mean absorption are σ^* and k^* , respectively. Within the flow, temperature variations T^4 can be described as a linear function of the temperature. This is performed by expanding and eliminating the higher order terms in Taylor's series about T_∞ , resulting in:

$$T^4 \approx -3T_\infty^4 + 4TT_\infty^3 \tag{2.8}$$

Using equations (10) and (11), Equation (3) reduces to:

$$\left(\rho c_p\right)_{hnf} (uT_x + vT_y) = k_{hnf} T_{yy} + \left(\frac{16\sigma^* T_\infty^3}{3k^*}\right) T_{yy} + \mu_{hnf} u_y^2 + Q_0 (T - T_\infty) \tag{2.9}$$

Applying the similarity variables (2.6)-(2.9) into Equations (2.1) – (2.3), the subsequent coupled ordinary differential equations are acquired, and the equation of continuity (2.1) is automatically satisfied.

$$f''' - (1 - \phi_1)^{2.5} (1 - \phi_2)^{2.5} \left\{ (1 - \phi_2) \left[(1 - \phi_1) + \phi_1 \left(\frac{\rho_{s1}}{\rho_f}\right) \right] + \phi_2 \left(\frac{\rho_{s2}}{\rho_f}\right) \right\} (f'^2 - ff'') - \frac{\sigma_{hnf}}{\sigma_f} (1 - \phi_1)^{2.5} (1 - \phi_2)^{2.5} M^2 f' - Kf' = 0 \tag{2.10}$$

$$\left(\frac{k_{hmf}}{k_f} + \frac{4R}{3}\right)\theta'' + \left\{(1-\phi_2)\left[(1-\phi_1) + \phi_1\left(\frac{(\rho c_p)_{s_1}}{(\rho c_p)_f}\right)\right] + \phi_2\left(\frac{(\rho c_p)_{s_2}}{(\rho c_p)_f}\right)\right\} \text{Pr} f \theta' + (1-\phi_1)^{-2.5} (1-\phi_2)^{-2.5} P_r E_c f''^2 + P_r Q \theta = 0 \tag{2.11}$$

Together with the dimensionless physical constraints listed below:

$$f'(0) = 1, f(0) = 0, \theta'(0) = \frac{-1}{\frac{k_{hmf}}{k_f}} B_i (1 - \theta(0)), f'(\infty) = 0, \theta(\infty) = 0 \tag{2.12}$$

where the superscripts signify η -related differentiation, $M^2 = \sigma_f B_0^2 / a \rho_f$ stand for the magnetic interaction variable, $K = \nu_f / ak$, $P_r = \mu_f (c_p)_f / \kappa_f$ stand for the Prandtl number, $Q = Q_0 / a(\rho c_p)_f$ represents the local heat generation, $R = 4\sigma^* T_\infty^3 / k^* k_f$ represents the radiation variable, $E_c = a^2 x^2 / (c_p)_f (T_w - T_\infty)$ stand for the local Eckert number and $B_i = h_f / k_f \sqrt{\frac{\nu_f}{a}}$ stand for the Boit number.

The important quantities, Skin friction coefficient, C_f , and Nusselt number, Nu_x , are given by:

$$C_f = \frac{\tau_w}{\rho_f u_w^2}, Nu_x = \frac{x q_w}{k_f (T_w - T_\infty)} \tag{2.13}$$

where the heat flux, q_w and Shear stress, τ_w , distinguished as:

$$\tau_w = \mu_{hmf} (u_y)_{y=0}, q_w = -k_{hmf} (T_y)_{y=0} + (q_r)_{y=0} \tag{2.14}$$

We get by plugging (14) into (13):

$$Cf_x Re_x^{\frac{1}{2}} = \frac{f''(0)}{(1-\phi_1)^{2.5} (1-\phi_2)^{2.5}}, \tag{2.15}$$

$$Nu_x Re_x^{-\frac{1}{2}} = -\left(\frac{k_{hmf}}{k_f} + \frac{4}{3} R\right) \theta'(0), \tag{2.16}$$

where Re_x , the local Reynolds number is defined as $Re_x = \frac{U_w x}{\nu_f}$.

3. Results and Discussion

The numerical solution of the problem from equation (10)-(12) for MHD MoS₂-Fe₃O₄/Blood towards a porous stretching surface with effecting thermal radiation and magnetic field was performed by Matlab's integrate function referred to as bvp4c solver. The subsequent section investigates the effects of the magnetic parameter (M), porous medium (K), heat absorption (Q), Radiative parameter (R), Eckert's number (E_C), and Biot number (Bi) on velocity and temperature distribution. In this article, we discussed two types of nanoparticles, Fe₃O₄ and MoS₂, as well as blood as the base fluid (Prandtl number is Pr=21). For the allocation

of velocity and temperature, the mechanism of blood over the stretching sheet is graphically presented, along with physical parameters. The figures show that the solid line represents a hybrid nanofluid consisting of $\text{MoS}_2\text{-Fe}_3\text{O}_4$, while the dotted line shows Fe_3O_4 . Figures 2 and 3 depict the consequences of magnetic parameter M on the velocity distribution $f'(\eta)$ and temperature distributions $\theta(\eta)$. Figure 2 depicts how velocity decreases as the magnetic parameter is increased. The transverse magnetic field generates a drag-like resistive force, which prefers to oppose fluid flow and slow down its velocity. Since the magnetic parameter enhances, the thickness of the boundary layer decreases. The velocity profile decreases as the magnetic effect rises, indicating that the magnetic field tends to slow the fluid's speed. While the fluid temperature amplifies, with an increase in magnetic values, as shown in Figure 3. Table 3 indicates that as the magnetic field rises, the skin friction coefficient declines due to the reduced velocity of the flow. Also, the magnetic field enhances the rate of heat dissipation decreases. It is pointed out that the nondimensional heat dissipation rate for $\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{blood}$ is greater than that of $\text{Fe}_3\text{O}_4/\text{blood}$.

Figure 4 exhibits the effect of porous media on $f'(\eta)$. The velocity of both nanofluid and hybrid nanofluid decreases as the porous media parameter is increased. Figure 5 demonstrates increasing values of the permeability coefficient as temperature rises. Figure 6 shows a temperature distribution comparison of a base fluid Blood, a nanofluid ($\text{Fe}_3\text{O}_4\text{-Blood}$), and a hybrid nanofluid ($\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$). The heat dissipation rate of $\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$ is greater than that of $\text{Fe}_3\text{O}_4/\text{Blood}$ and base fluid. The nanoparticles physically disperse energy as heat. The addition of more nanoparticles could increase the temperature by exerting more energy. The influence of heat absorption against dimensionless temperature is revealed in Figure 7. It is quite clear that increasing the heat absorption parameter causes an increase in temperature. These findings are qualitatively consistent with expectations, as the effect of internal heat generation is to increase the frequency of heat transport to the fluid by raising the temperature of both hybrid nanofluid and nanofluid.

The dimensionless temperature profile for the radiation parameter is plotted in Figure 8. It has been observed that the temperature profiles enhance with rising values of thermal radiation. Because the thickness of the thermal protective layer magnifies with increasing thermal radiation, the effect of thermal radiation enhances heat transfer. As a result, it is suggested that radiation be reduced in order for the cooling process to move more quickly. We also noted that the heat transfer in the case of the $\text{Fe}_2\text{O}_3\text{-Blood}$ is comparatively less than $\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$. Figure 9 depicts the significance of the Eckert number. It can be seen that increasing Ec causes an increase in heat transfer. Figure 10 shows the effect of Bi on temperature profile; when viewing this figure, the temperature of $\text{MoS}_2\text{-Fe}_3\text{O}_4/\text{Blood}$ and $\text{Fe}_2\text{O}_3\text{-Blood}$ increases with the increasing parameter Bi . Table 3 shows that reduced skin friction decreases with the enlarging M , Ec , Bi , and volume fraction coefficient of Fe_3O_4 . But the drag factor is indistinctly large for a hybrid Nanofluid. The proportional increases in the heat transfer rate for changes in Fe_3O_4 nanoparticles volume fraction ϕ_2 from 0.15, 0.20, 0.25, and 0.30 enhance heat transfer of both nanofluid and hybrid nanofluid. This demonstrates that, compared to other traditional fluids, the hybrid nanofluid improves the heat transfer rate more efficiently.

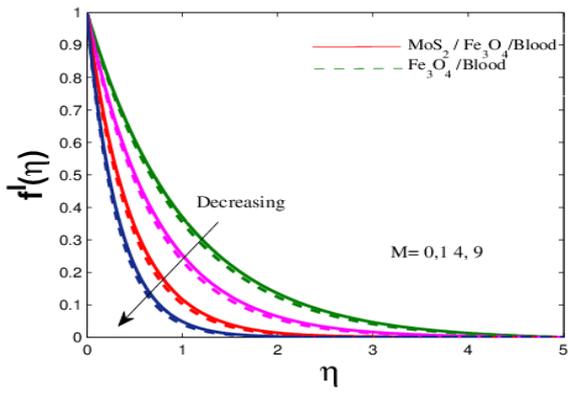


Figure 2. Effects of $f'(\eta)$ on M variations.

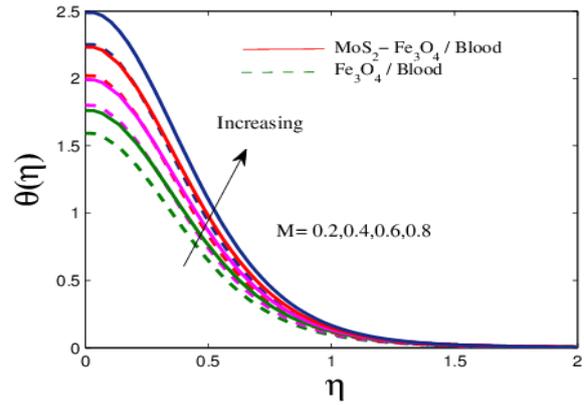


Figure 3. Effects of $\theta(\eta)$ on M adaptations.

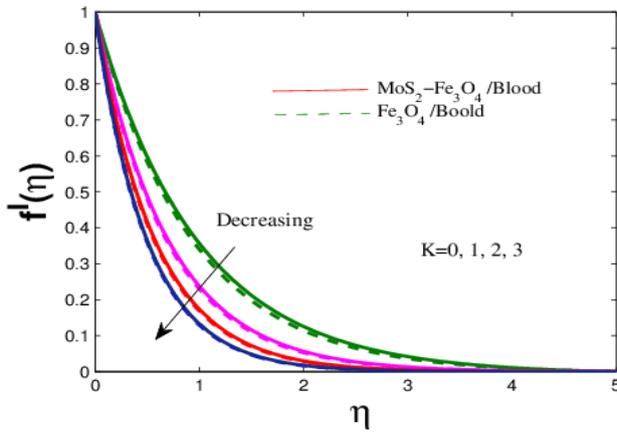


Figure 4. Effects of $f'(\eta)$ on K variations.

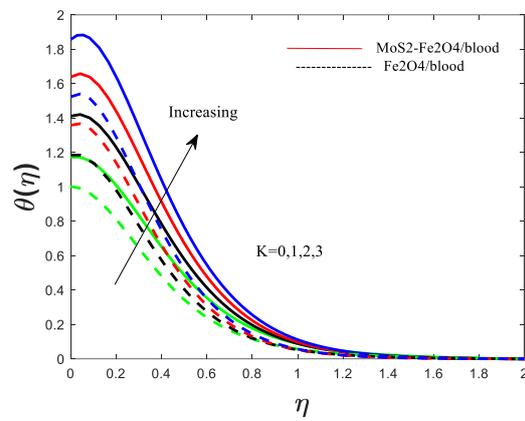


Figure 5. Effects of $\theta(\eta)$ on K variations.

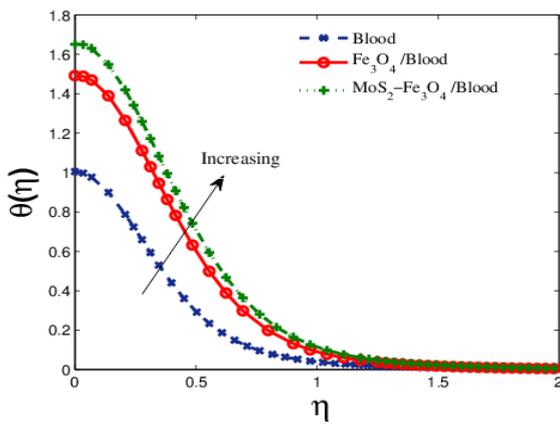


Figure 6. The effects of various Fluids.

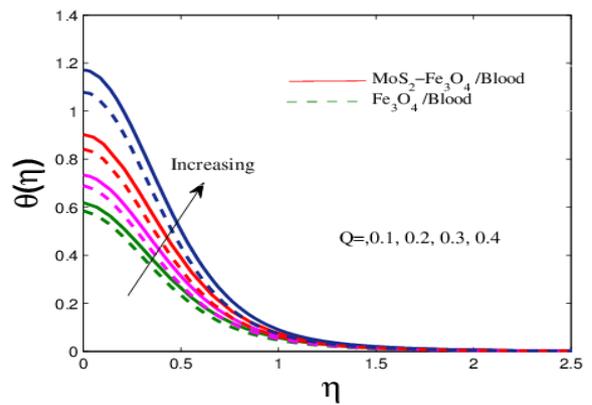


Figure 7. Impacts of Q in $\theta(\eta)$.

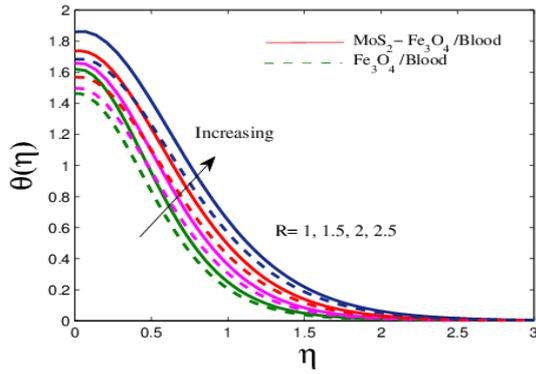


Figure 8. Consequences of R in $\theta(\eta)$.

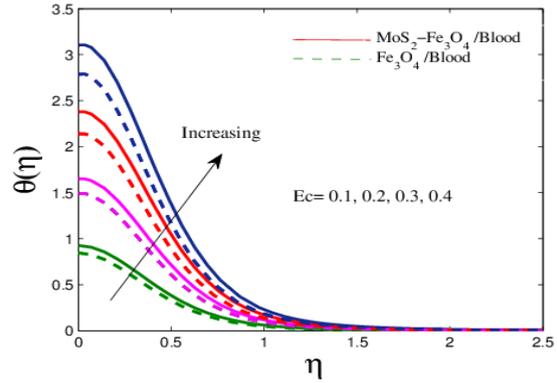


Figure 9. Consequences of Ec in $\theta(\eta)$.

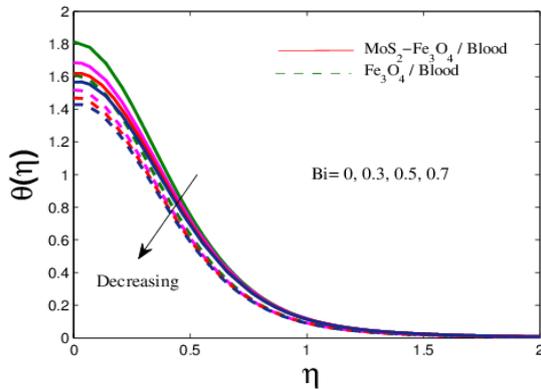


Figure 10. Consequences of Bi $\theta(\eta)$.

Table 1. $Cf_x Re_x^{\frac{1}{2}}$ and $Nu_x Re_x^{\frac{1}{2}}$ for $MoS_2 - Fe_3O_4 / Blood$ and $Fe_3O_4 / Blood$.

M	Bi	R	Ec	ϕ_2	$Cf_x Re_x^{\frac{1}{2}}$		$Nu_x Re_x^{\frac{1}{2}}$	
					$Fe_3O_4 / Blood$	$MoS_2 - Fe_3O_4 / Blood$	$Fe_3O_4 / Blood$	$MoS_2 - Fe_3O_4 / Blood$
1	2	0.01	0.001	0.15	-1.987448	-2.589179	1.278832	1.319292
3					-2.853769	-3.739153	1.254773	1.291414
5					-3.512798	-4.611014	1.235339	1.268787
7					-4.066390	-5.342442	1.218302	1.248877
	4				-3.799689	-4.990147	1.767688	1.838830
	6				-2.853769	-3.739153	2.149171	2.265404
0.3	8				-1.578048	-2.042269	2.477270	2.644910
		0.03			-2.853769	-3.739153	1.276455	1.309406
		0.05			-1.578048	-2.042269	1.335186	1.369804
		0.07			-1.391268	-1.791354	1.340245	1.375575
			0.002		-2.853769	-3.739153	1.260162	1.317244
			0.004		-3.512798	-4.611014	1.245637	1.262721

					$Cf_x Re_x^{\frac{1}{2}}$		$Nu_x Re_x^{\frac{1}{2}}$	
M	Bi	R	Ec	ϕ_2	$Fe_3O_4 /$ <i>Blood</i>	$MoS_2 - Fe_3O_4$ <i>/Blood</i>	$Fe_3O_4 /$ <i>Blood</i>	$MoS_2 - Fe_3O_4$ <i>/Blood</i>
			0.006		-3.799689	-4.990147	1.209026	1.216727
				0.20	-4.310300	-5.653408	1.239496	1.269300
				0.25	-4.910118	-6.433505	1.242014	1.271446
6	2	0.02		0.30	-5.622427	-7.360897	1.244533	1.273553

4. Conclusions

In this study, a numerical investigation of $MoS_2-Fe_3O_4/Blood$ towards a porous stretching sheet under the nose of thermal radiation and magnetic field was discovered. The impact of magnetic parameters, porous medium, heat absorption, Radiation parameter, Eckert number, Biot number, and nanoparticle volume fraction on the $Cf_x Re_x^{\frac{1}{2}}$ and $Nu_x Re_x^{\frac{1}{2}}$ as well as velocity and temperature profiles has been investigated in this study. The findings are as follows: By virtue of an increase, the magnetic parameter reduces the skin friction coefficient, velocity, and Nusselt number for $MoS_2-Fe_3O_4/Blood$ and $Fe_3O_4/blood$, while temperature increases; The heat transfer rate of hybrid nanofluid $MoS_2-Fe_3O_4/blood$ is higher than those of $Fe_3O_4/blood$; The temperature is also increasing by increasing the heat source and radiation parameters; As the Biot number Bi and Eckert number Ec increase, so does the thermal; The skin friction values increase as the values of thermal radiation and Ec increase, whereas the frequency of occurrence of heat transfer decreases as the values of M and Ec increase.

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Conflicts of Interest

The authors declare no conflict of interest

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